

## Simulation of $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$ Work Function Change-Based Sensor of $\text{H}_2$ Gas

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**ABSTRACT:** Chemical reactions simulation in detecting hydrogen gas ( $\text{H}_2$ ) on  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$  sensor surface based on work function change ( $\Delta\phi$ ) has been conducted. The simulation result is compared with laboratory results of detecting  $\text{H}_2$  gas. Three chemical reactions contained three coverages, H coverage ( $\theta_{\text{H}}$ ), O coverage ( $\theta_{\text{O}}$ ), and  $\text{H}_2\text{O}$  coverage ( $\theta_{\text{H}_2\text{O}}$ ). The simulation was run using MATLAB. This research can find the reaction parameter values such as the Arrhenius coefficient of  $\text{H}_2\text{O}$  forming reaction on Pt ( $\mathcal{V}_{\text{fPt}}$ ),  $\text{H}_2\text{O}$  forming reaction on Au ( $\mathcal{V}_{\text{fAu}}$ ), i.e.,  $\text{H}_2\text{O}$  dissociation on Au ( $\mathcal{V}_{\text{dAu}}$ ),  $\text{O}_2$  desorption on Ti ( $\mathcal{V}_{\text{dT}}$ ),  $\text{H}_2\text{O}$  forming reaction on Ti ( $\mathcal{V}_{\text{fTi}}$ ), and  $\text{H}_2\text{O}$  dissociation on Ti ( $\mathcal{V}_{\text{dTi}}$ ), i.e.,  $7.5 \times 10^{14} \text{ s}^{-1}$ ,  $9.85 \times 10^{15} \text{ s}^{-1}$ ,  $3.25 \times 10^{15} \text{ s}^{-1}$ ,  $7.11 \times 10^{15} \text{ s}^{-1}$ ,  $3.425 \times 10^{15} \text{ s}^{-1}$  and  $2.725 \times 10^{15} \text{ s}^{-1}$ , respectively. The simulation results also have the same trend as the laboratory results. However, the contact potential difference (CPD) simulation result, i.e.,  $-240 \text{ mV}$ , is not the same as the laboratory result,  $(-297 \pm 9) \text{ mV}$ . In addition, this simulation also obtained approximation coverage for atoms/molecules on  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$  surface, i.e.,  $\theta_{\text{H}} = 0.665154 \text{ Mono Layer (ML)}$ ;  $\theta_{\text{O}} = 1.5621 \times 10^{-6} \text{ ML}$ ; and  $\theta_{\text{H}_2\text{O}} = 5.41676 \times 10^{-5} \text{ ML}$ .

**Keywords:** CPD, gas sensor, hydrogen, simulation, work function change

## 1. INTRODUCTION

Hydrogen (H) has been used in industry since the mid-20th century, such as a mixture of rocket fuel, hydrochloride production, iron ore reduction, fat hydrogenation and fuel cell.<sup>1</sup> H is the most abundant element, with 75% of the total air element. H is colourless, odourless, non-metallic, single valency and flammable at 4% concentrations in free air.<sup>2</sup> This gas is chemically active and rarely found in free form. H exists in compounds with other elements, such as oxygen in water (H<sub>2</sub>O) or carbon in methane (CH<sub>4</sub>). Hydrogen gas (H<sub>2</sub>) will explode by itself at 560°C.<sup>3</sup>

The risk of using H could be minimised if a sensor gas could detect a gas leak. The gas sensor is a chemical sensor consisting of an active layer and transducer, which is used to convert chemical information into electronic signals such as current, frequency, and voltage.<sup>4</sup> The capability of gas sensors depends on several parameters, such as sensitivity, selectivity, detection limit, response time and recovery time.<sup>5</sup> There are two working mechanism types of gas sensors based on resistivity and work function change.<sup>6</sup> The sensor uses the value of material work function change ( $\Delta\phi$ ) caused by coming gases (also called contact potential difference/CPD) as the sensor signal. An example of a gas sensor based on a  $\Delta\phi$  transducer is the floating gate field effect transistor (FGFET). The advantages of this method were the more straightforward process and fewer steps than other methods.<sup>7</sup>

Research on H<sub>2</sub> sensors has been carried out in platinum (Pt), nickel (Ni), titanium dioxide (TiO<sub>2</sub>), zinc oxide (ZnO), palladium-gold alloy (PdAu), tin(IV) oxide (SnO<sub>2</sub>) and Pt<sub>80</sub>Au<sub>14</sub>Ti<sub>6</sub>.<sup>8–14</sup> Research of H sensors using Pt<sub>80</sub>Au<sub>14</sub>Ti<sub>6</sub> based on CPD properties shows the signal ( $-297 \pm 9$ ) mV for 15,000 ppm H<sub>2</sub>. Pt<sub>80</sub>Au<sub>14</sub>Ti<sub>6</sub> also has cross-sensitivity to the 50 ppm NH<sub>3</sub> and five ppm NO<sub>2</sub> with its signal, i.e., ( $100 \pm 20$ ) mV and ( $50 \pm 10$ ) mV.<sup>14</sup> Another H<sub>2</sub> sensor which is using FGFET was also fabricated by Senft.<sup>15</sup> Senft used Pt for the sensitive layer. The sensor signal is 600 mV for 20,000 ppm of H<sub>2</sub>. When H<sub>2</sub> is increased linearly, the sensor signal raises logarithmic.

Three parameters are employed in the working mechanism of the gas sensor, i.e., the sticking coefficient, Arrhenius coefficient, and activation energy in each reaction. Since material parameter values are inferior, an optimisation process is needed to get the parameter's value.

The restriction is needed for the simulation in this study. It only uses three reactions between gas and material surface (H<sub>2</sub> adsorption, O<sub>2</sub> adsorption, and H and O reaction). No simulation has been carried out from the literature studies on this topic.

## 2. METHODS

### 2.1 Tools

The tool used in this study is a computer set with MATLAB software for simulations.

### 2.2 Reaction Mechanism

In research of  $H_2$  detection in Pt, there are seven reactions between coming gases and material surface.<sup>8</sup> Those reactions are written in Equation (2.1) to Equation (2.3). This simulation uses only three reactions,  $H_2$  adsorption,  $O_2$  adsorption and a reaction between H and O on the surface.



where S is the surface site. To calculate coverage ( $\theta$ ) change rate by gas on the surface in the adsorption process (atom/s or molecule/s) was started by calculating the adsorption rate in Equation (2.4).<sup>16</sup>

$$r_a = \frac{dN_{ads}}{dt} \quad (2.4)$$

$N_{ads}$  is the number of atoms or molecules (on the surface), which could be defined in Equation (2.5).

$$N_{ads} = \sigma\theta \quad (2.5)$$

where  $\sigma$  is the surface atomic density of the layer (atom/m<sup>2</sup>), and  $\theta$  is gas coverage on the surface (in Mono Layer or ML). The value of  $r_a$  also depends on the molecular flux in the material surface ( $F$ , m<sup>-2</sup> s<sup>-1</sup>) based on Hertz-Knudsen law, as shown in Equation (2.6).<sup>16</sup>

$$F = -\frac{P}{\sqrt{2\pi mkT^*}} \quad (2.6)$$

Sticking probability ( $S$ , dimensionless) has presented in Equation (2.7).

$$S = S_0(1 - \theta)^{\gamma} \exp\left(-\frac{E_a}{kT}\right) \quad (2.7)$$

where  $P$  is gas pressure (Pa),  $m$  is the molecular gas mass (kg),  $k$  is Boltzmann constant ( $1.38 \times 10^{-23} \text{ JK}^{-1}$ ),  $T$  is the temperature (K),  $S_0$  is the initial sticking coefficient when coverage gas is still zero, and  $z$  is 1 for an undissociated gas and 2 for dissociated gas. According to Equation (2.6) and Equation (2.7), it can be seen that the temperature contributes to the calculation. The temperature contribution is not only in those equations but also for all the equations, which consist of activation energy. Then, if Equation (2.4) to Equation (2.7) are combined, gas  $\theta$  rate change in the adsorption process is obtained as revealed in Equation (2.8).<sup>14</sup>

$$\frac{d\theta}{dt} = \frac{S_0(1-\theta)^z P}{\sigma \sqrt{2\pi m k T}} \exp\left(-\frac{E_a}{kT}\right) \quad (2.8)$$

When atoms or molecules of gas A (on the surface) are reacted with gas B (on the surface) to become AB molecules, based on the Langmuir-Hinshelwood mechanism, the  $\theta$  rate of AB gas can be calculated using Equation (2.9).<sup>15,17</sup>

$$\frac{d\theta_{AB}}{dt} = \nu_r \exp\left(-\frac{E_a}{kT}\right) \theta_A \theta_B \quad (2.9)$$

where  $\nu_r$  is the Arrhenius coefficient or reaction frequency of A and B (reaction/s),  $E_r$  is the activation energy of the reaction between A and B gases (eV) and  $\theta_A \theta_B$  is  $\theta$  of A and B gases on the surface.

If a molecule (e.g., AB) dissociates into A and B (on the surface), then the  $\theta$  rate change of gas A as given in Equation (2.10).<sup>15</sup>

$$\frac{d\theta_A}{dt} = \nu_{\text{diss}} \exp\left(-\frac{E_{\text{diss}}}{kT}\right) \theta_{AB} \quad (2.10)$$

where  $\nu_{\text{diss}}$  is the Arrhenius coefficient or dissociation frequency AB (dissociation/s),  $E_{\text{diss}}$  is AB dissociation energy (eV), and  $\theta_{AB}$  is AB molecule coverage.

Adsorbed molecules on the surface will be rereleased when given the desorption energy ( $E_d$  in eV).  $\theta$  rate change can be determined using Equation (2.11).<sup>14</sup>

$$\frac{d\theta}{dt} = \nu_d \exp\left(-\frac{E_d}{kT}\right) \theta \quad (2.11)$$

where  $\nu_d$  is the Arrhenius coefficient or desorption frequency (desorption/s).

Afterwards, the work function ( $\phi$ ) of the material depends on the gas  $\theta$ . The work function of Pt has already been known as presented in Equation (2.12) to Equation (2.15).<sup>18-20</sup>

$$\phi_{\text{H-Pt}} = -0.23\theta_{\text{H}}^{4/3} \text{ eV} \quad (2.12)$$

$$\phi_{O-Pt} = 2.663\theta_o \text{ eV, if } \theta_o < 0.0086 \text{ ML} \quad (2.13)$$

$$\phi_{O-Pt} = (0.557\theta_o + 0.184) \text{ eV, if } \theta_o \geq 0.0086 \text{ ML} \quad (2.14)$$

$$\phi_{H_2O-Pt} = (-1.1798\theta_{H_2O}^3 + 3.3114\theta_{H_2O}^2 - 1.1798\theta_{H_2O} - 0.0108) \text{ eV} \quad (2.15)$$

In Gottfried's research, the work function of Au with oxygen gas was formulated in Equation (2.16).<sup>21</sup>

$$\phi_{O-Au} = \frac{1.7 \times 10^{19} \times 3.3 \times 10^{-30} \theta_o}{8.85 \times 10^{12} (1 + 9 \times 1.5 \times 10^{-24} \times 10^{-6} \times (1.7 \times 10^{19} \theta_o))} \text{ eV} \quad (2.16)$$

For Ti material, work function formula ( $\phi$ ) of O and H<sub>2</sub>O as given in Equation (2.17) and Equation (2.18).<sup>22,23</sup>

$$\phi_{O-Ti} = 0.586\theta_o - 0.0415 \text{ eV} \quad (2.17)$$

$$\phi_{H_2O-Ti} = -0.49\theta_{H_2O} \text{ eV} \quad (2.18)$$

Since  $\phi_{H-Au}$ ,  $\phi_{H_2O-Au}$  and  $\phi_{H-Ti}$  are not available, the work function value was made equal to coverage ( $\theta$ ) as revealed in Equation (2.19) to Equation (2.21),

$$\phi_{H-Au} = \theta_{H-Au} \text{ eV} \quad (2.19)$$

$$\phi_{H_2O-Au} = \theta_{H_2O-Au} \text{ eV} \quad (2.20)$$

$$\phi_{H-Ti} = \theta_{H-Ti} \text{ eV} \quad (2.21)$$

Because Pt<sub>80</sub>Au<sub>14</sub>Ti<sub>6</sub> is a mixture of three materials, the work function of each material is as written in Equation (2.22) – Equation (2.24),

$$\phi_{Pt} = \phi_{H-Pt} + \phi_{O-Pt} + \phi_{H_2O-Pt} \quad (2.22)$$

$$\phi_{Au} = \phi_{H-Au} + \phi_{O-Au} + \phi_{H_2O-Au} \quad (2.23)$$

$$\phi_{Ti} = \phi_{H-Ti} + \phi_{O-Ti} + \phi_{H_2O-Ti} \quad (2.24)$$

Then, the total work function value ( $\phi_{Total}$ ) is based on the percentage of each material as given in Equation (2.25).

$$\phi_{Total} = 80\%\phi_{Pt} + 14\%\phi_{Ti} + 6\%\phi_{Ti} \quad (2.25)$$

Finally, the relation between work function and CPD is written in Equation (2.26).<sup>24</sup>

$$CPD = \frac{\phi_{\text{Total}}}{|e|} \quad (2.26)$$

### 2.3 Fitting of Experimental Graph

Before the parameter optimisation process is carried out, it is necessary to approach the experimental graph of Marjunus with fitting.<sup>14</sup> It calculates the error between the simulation and the experimental results.

### 2.4 Parameter Optimisation

The simulation requires 36 parameters for the H<sub>2</sub> gas detection process, as shown in Table 1.<sup>25–44</sup> The six parameters were Arrhenius coefficients i.e.,  $v_{f3Pt}$ ,  $v_{f3Au}$ ,  $v_{r3Au}$ ,  $v_{d2Ti}$ ,  $v_{f3Ti}$  and  $v_{r3Ti}$ . Their values would be obtained by finding the smallest error average value between the simulation and the experimental results. However, six parameters are unknown, so an optimisation process was needed to get the best deal.

Table 1. Data of H<sub>2</sub> gas detection parameter on Pt<sub>80</sub>Au<sub>14</sub>Ti<sub>6</sub> surface.

$S_0$ dan Arrhenius coefficient ( $s^{-1}$ )		Activation energy (eV)	
Forward reaction	Reverse reaction	Forward reaction	Reverse reaction
$S_{01Pt} = 0.046$	$v_{d1Pt} = 6.0 \times 10^{12}$	$E_{f1Pt} = 0.13$	$E_{r1Pt} = 0.91$
$S_{02Pt} = 0.07 \times (300/T)$	$v_{d2Pt} = 8.0515 \times 10^{12}$	$E_{f2Pt} = 0.53$	$E_{r2Pt} = 2.20 - 966.0622\theta_o$
$v_{f3Pt} = -$	$v_{r3Pt} = 3.1 \times 10^{15}$	$E_{f3Pt} = 0.42$	$E_{r3Pt} = 0.68$
$S_{01Au} = 0.5$	$v_{d1Au} = 1.0 \times 10^{13}$	$E_{f1Au} = 0.16$	$E_{r1Au} = 0.68$
$S_{02Au} = 0.005$	$v_{d2Au} = 1.0 \times 10^{11}$	$E_{f2Au} = 2.17$	$E_{r2Au} = 1.6$
$v_{f3Au} = -$	$v_{r3Au} = -$	$E_{f3Au} = 0.92$	$E_{r3Au} = 2.3$
$S_{01Ti} = 0.17$	$v_{d1Ti} = 2.1 \times 10^7$	$E_{f1Ti} = 0.5$	$E_{r1Ti} = 0.51$
$S_{02Ti} = 0.62$	$v_{d2Ti} = -$	$E_{f2Ti} = 1.15$	$E_{r2Ti} = 0.152$
$v_{f3Ti} = -$	$v_{r3Ti} = -$	$E_{f3Ti} = 1.09$	$E_{r3Ti} = 1.10$

### 2.5 Re-optimisation Parameters

After the value of  $v_{f3Pt}$ ,  $v_{f3Au}$ ,  $v_{r3Au}$ ,  $v_{d2Ti}$ ,  $v_{f3Ti}$  and  $v_{r3Ti}$  were obtained, the re-optimisation process was required for them to check the change value of each parameter. If the value was changed, the final value was acquired by the initial optimisation and re-optimisation average.

## 2.6 Final Simulation

The final process of this research was simulating all parameters that have been optimised. The final values of all parameters were entered into the program to simulate Matlab. This step obtained  $\theta$  value, total work function ( $\phi_{\text{Total}}$ ), and *CPD*. *CPD* (V) graph would be plotted against time ( $t$ ), and then the *CPD* graph was compared with Marjunus's laboratory result.<sup>14</sup>

## 3. RESULTS AND DISCUSSION

### 3.1 Differential Equation

This simulation used three reactions:  $\text{H}_2$  adsorption,  $\text{O}_2$  adsorption, and H with O reactions, Equation (2.12) to Equation (2.14). Those reactions were made into the coupled first order ordinary differential equations as written in Equation (4.1) to Equation (4.3) to obtain coverage value ( $\theta$ ), work function change ( $\Delta\phi$ ), and *CPD*.

$$\frac{d\theta_{\text{H}}}{dt} = r_{\text{f1}}F_{\text{H}_2} - r_{\text{b3}}\theta_{\text{H}}^2\theta_{\text{O}} + r_{\text{r3}}\theta_{\text{H}_2\text{O}} - r_{\text{f1}}\theta_{\text{H}}^2 \quad (3.1)$$

$$\frac{d\theta_{\text{O}}}{dt} = 2r_{\text{f2}}F_{\text{O}_2} - r_{\text{b3}}\theta_{\text{H}}^2\theta_{\text{O}} + r_{\text{r3}}\theta_{\text{H}_2\text{O}} - 2r_{\text{f2}}\theta_{\text{O}}^2 \quad (3.2)$$

$$\frac{d\theta_{\text{H}_2\text{O}}}{dt} = r_{\text{b3}}\theta_{\text{H}}^2\theta_{\text{O}} - r_{\text{r3}}\theta_{\text{H}_2\text{O}} \quad (3.3)$$

where  $F$  is the adsorption factor, and  $r$  is the gas  $\theta$  rate described in Equation (3.4) to Equation (3.6).<sup>15</sup>

$$F_x = (1 - \theta_x)^z \frac{P}{\sqrt{2\pi mkT}} \quad (3.4)$$

$$r_{\text{f}} = S_{0x} \exp\left(-\frac{E_{\text{f}}}{kT}\right) \quad (3.5)$$

$$r_{\text{for r}} = \nu_{\text{f or r}} \exp\left(-\frac{E_{\text{f}}}{kT}\right) \quad (3.6)$$

where  $x$  index in Equation (3.4) represents the symbol of coming gases at  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$  surface,  $z$  is 1 for undissociated gas and 2 for dissociated gas,  $P$  is gas pressure (Pa),  $m$  is gas mass (kg),  $k$  is Boltzman constant,  $T$  is the temperature (K), and  $\sigma$  is atomic density on the surface (value for Pt, Au and Ti are  $1.3 \times 10^{19}$  atom/ $\text{m}^2$ ,  $1.2 \times 10^{19}$  atom/ $\text{m}^2$ , and  $2.3 \times 10^{19}$  atom/ $\text{m}^2$ , respectively).<sup>14</sup> Equation (3.5) was only used to find the ( $\theta$ ) rate of the  $\text{H}_2$  and  $\text{O}_2$  adsorption process (forward reaction of Equation [2.2] and Equation [2.3]). Equation (3.6) was used to calculate the  $\theta$  rate except  $\text{H}_2$  and  $\text{O}_2$  gas adsorption process. Index f in Equation (3.5) and

Equation (3.6) describes the forward reaction,  $r$  index in Equation (3.6) represents the reverse reaction.

### 3.2 Fitting of Experimental Graph

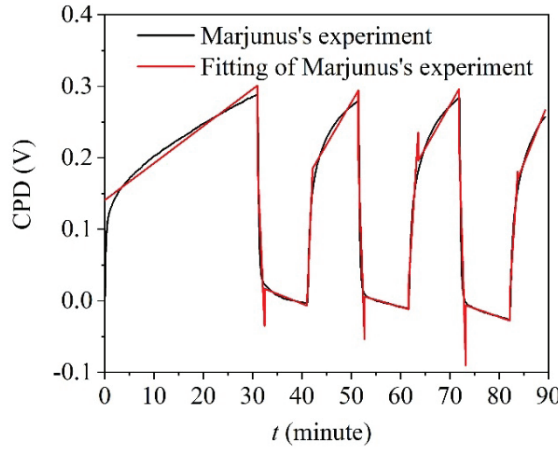


Figure 1: Fitting of Marjunus's graph.<sup>14</sup>

The fitting graph is presented in Figure 1. Each trend graph was fitted with has R-Square (COD) value which described the correlation factor between the laboratory result and its fitting. The average R-Square (COD) value is 0.89518, which is confirmed that the fitting curve approaches with laboratory results.

### 3.3 Parameter Optimisation Results

After the fitting process was completed, six parameters ( $v_{f3\text{Pt}}$ ,  $v_{f3\text{Au}}$ ,  $v_{r3\text{Au}}$ ,  $v_{d2\text{Ti}}$ ,  $v_{f3\text{Ti}}$ , and  $v_{r3\text{Ti}}$ ) were optimised to find values with the smallest CPD error of those parameters. Before the optimisation process starts, the initial values must be given to those parameters. The results of optimisation are presented in Figure 2 to Figure 7.



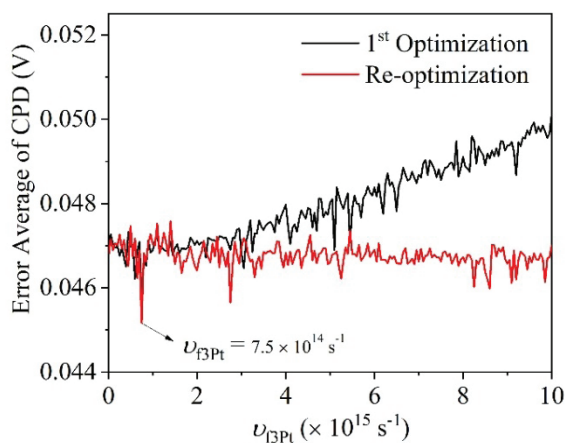


Figure 2: Optimisation of  $v_{f3Pt}$  with  $5 \times 10^{13} \text{ s}^{-1}$  partition length.

Figure 2 shows the initial optimisation and re-optimisation of the Arrhenius coefficient of the  $\text{H}_2\text{O}$  forming reaction on Pt ( $v_{f3Pt}$ ). The smallest error average (0.045169 V) of the initial optimisation occurs at the exact value of  $v_{f3Pt}$  of the re-optimisation, i.e., at  $7.5 \times 10^{14} \text{ s}^{-1}$ .

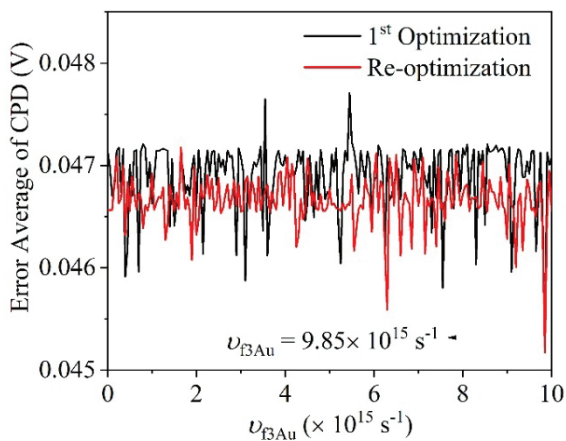


Figure 3: Optimisation of  $v_{f3Au}$  with  $5 \times 10^{13} \text{ s}^{-1}$  partition length.

Then, the smallest error average (0.045169 V) of the initial optimisation and re-optimisation of H<sub>2</sub>O forming reaction on Au ( $\nu_{\text{r3Pt}}$ ) occurs also at the same value, i.e.,  $9.85 \times 10^{15} \text{ s}^{-1}$  (Figure 3).

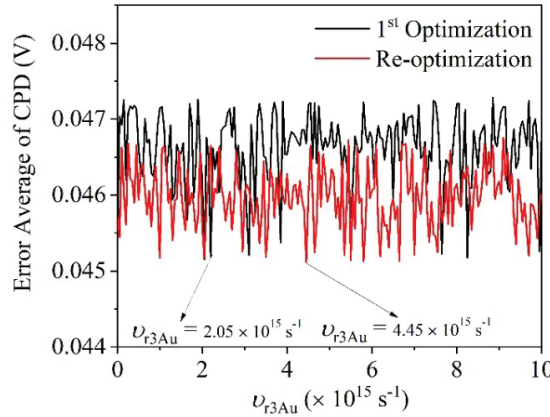


Figure 4: Graphic optimisation for with  $5 \times 10^{13} \text{ s}^{-1}$  partition length.

On the other hand, Figure 4 presents the different values for Arrhenius coefficient dissociation of H<sub>2</sub>O on Au ( $\nu_{\text{r3Au}}$ ) at the initial optimisation and re-optimisation (at the smallest error average), i.e.,  $4.45 \times 10^{15} \text{ s}^{-1}$  and  $2.05 \times 10^{15} \text{ s}^{-1}$ . The average/final value for  $\nu_{\text{r3Au}}$  is  $3.25 \times 10^{15} \text{ s}^{-1}$ .

The same properties as  $\nu_{\text{r3Au}}$  also happen for the Arrhenius coefficient of:

1. O<sub>2</sub> desorption on Ti ( $\nu_{\text{d2Ti}}$ ), the initial optimisation and re-optimisation values are  $6.88 \times 10^{14} \text{ s}^{-1}$  and  $7.34 \times 10^{14} \text{ s}^{-1}$ , respectively, which gives the average, i.e.,  $7.11 \times 10^{14} \text{ s}^{-1}$  (Figure 5).
2. H<sub>2</sub>O forming reaction on Ti ( $\nu_{\text{f3Ti}}$ ), the initial optimisation and re-optimisation values are  $5.65 \times 10^{15} \text{ s}^{-1}$  and  $1.2 \times 10^{15} \text{ s}^{-1}$ , respectively, which results in the average value at  $3.425 \times 10^{15} \text{ s}^{-1}$  (Figure 6).
3. In dissociation of H<sub>2</sub>O on Ti ( $\nu_{\text{r3Ti}}$ ), the initial optimisation and re-optimisation values are  $2.35 \times 10^{15} \text{ s}^{-1}$  and  $3.1 \times 10^{15} \text{ s}^{-1}$ , respectively, which results in the average value at  $2.725 \times 10^{15} \text{ s}^{-1}$  (Figure 7).

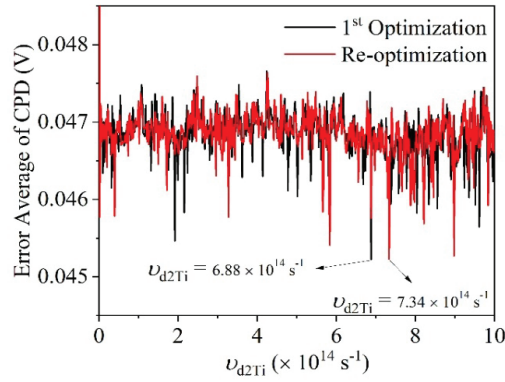


Figure 5: Graphic optimisation for  $\nu_{d2Ti}$  with  $2 \times 10^{12} \text{ s}^{-1}$  partition length.

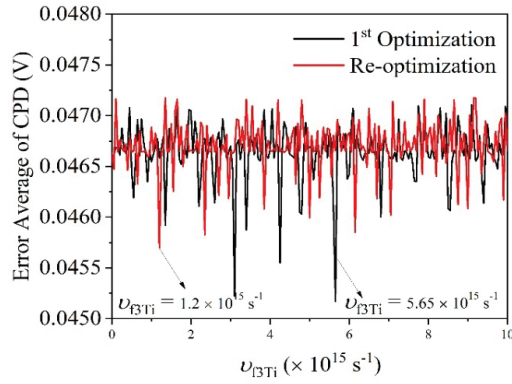


Figure 6: Graphic optimisation for  $\nu_{f3Ti}$  with  $5 \times 10^{13} \text{ s}^{-1}$  partition length.

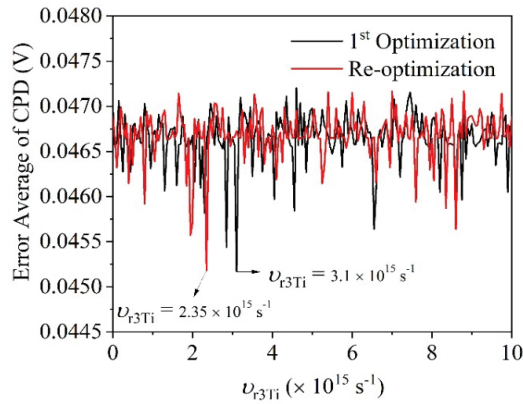


Figure 7: Graphic optimisation for  $\nu_{r3Ti}$  with  $5 \times 10^{13} \text{ s}^{-1}$  partition length.

The parameter values invented in this work (Table 2) complete the previous research from other scientists, as presented in Table 1. The recapitulation of those values is shown in Table 2. These values are one of the primary inventions of this research. After these values are obtained, it means that all of the parameter values which are needed for the final simulation are available.

Table 2. The final value of six parameters after initial optimisation and re-optimisation.

Parameter	Initial Optimisation (s <sup>-1</sup> )	Re-optimisation (s <sup>-1</sup> )	Final value (s <sup>-1</sup> )
$v_{\text{fPt}}$	$7.5 \times 10^{14}$	$7.5 \times 10^{14}$	$7.5 \times 10^{14}$
$v_{\text{fAu}}$	$9.85 \times 10^{15}$	$9.85 \times 10^{15}$	$9.85 \times 10^{15}$
$v_{\text{fTi}}$	$2.05 \times 10^{15}$	$4.45 \times 10^{15}$	$3.25 \times 10^{15}$
$v_{\text{d2Ti}}$	$6.88 \times 10^{14}$	$7.34 \times 10^{14}$	$7.11 \times 10^{14}$
$v_{\text{fTi}}$	$5.65 \times 10^{15}$	$1.2 \times 10^{15}$	$3.425 \times 10^{15}$
$v_{\text{fTi}}$	$3.1 \times 10^{15}$	$2.35 \times 10^{15}$	$2.725 \times 10^{15}$

### 3.4 Final Simulation

After four steps in this research have been completed, the final process is the final simulation. The final simulation is a computation involving all parameter values from the literature study and this research. The CPD graph in this process will be compared with Marjunus's laboratory result.<sup>14</sup> The result is shown in Figure 8. According to Figure 8, in Marjunus's research, CPD change of Pt<sub>80</sub>Au<sub>14</sub>Ti<sub>6</sub> when 15,000 ppm H<sub>2</sub> gas is exposed on the surface sample, i.e.,  $(-297 \pm 9)$  mV.<sup>14</sup> Based on the simulation results, the CPD change of Pt<sub>80</sub>Au<sub>14</sub>Ti<sub>6</sub> is  $-240$  mV, which means there is still a tiny difference between the simulation and laboratory results. But this simulation seems successful because the trend of simulation results is almost the same as the laboratory result.

Additionally, Figure 8 also shows the response and recovery time of the sensor signal. It proves again that the simulation result confirms the laboratory signal. The response/recovery time of simulation results is in agreement with the laboratory signals. When the H<sub>2</sub> is switched on, the laboratory and simulation signal decrease immediately. However, the laboratory signals are not saturated as the simulation signal, the laboratory signal increases as well as the simulation signal when the H<sub>2</sub> is switched off.

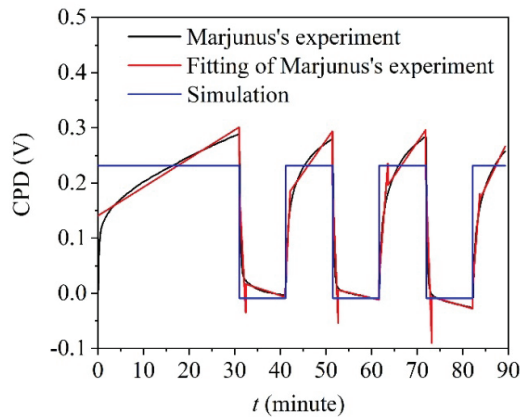
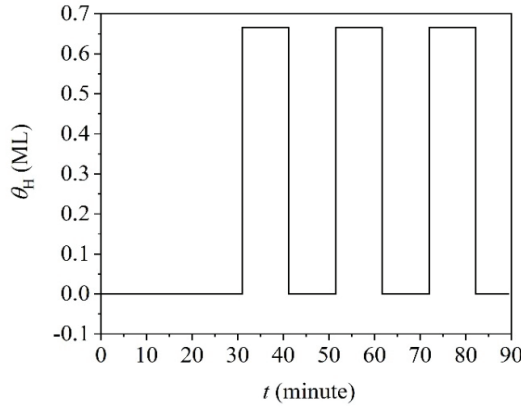


Figure 8: Comparison of  $H_2$  signal sensor simulation and Marjunus's experiment.<sup>14</sup>

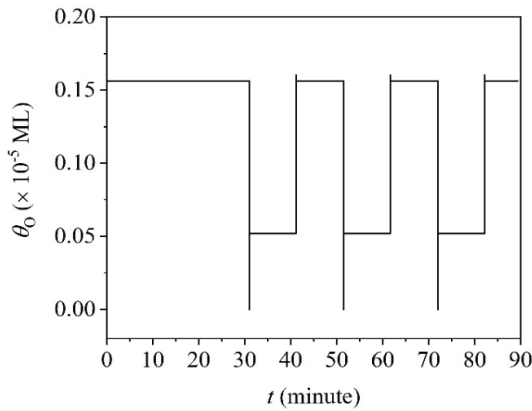
Several factors that cause the difference in CPD between simulation and laboratory results are as follows:

- The involved gases in the simulation process are still incomplete.
- Three involved reactions in the simulation process are fewer than in reality (experiments).
- There are still three of nine work function ( $\phi$ ) formulations that are unknown, so those formulations are approached as presented in Equation (2.19) to Equation (2.21).

Furthermore, another advantage of this simulation is calculating the atoms/molecules of gases on the surface of  $Pt_{80}Au_{14}Ti_6$ . H coverage ( $\theta_H$ ) on the surface during the gas detection process can be seen in Figure 9.

Figure 9:  $\theta_H$  on  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$  surface.

Based on Figure 9,  $\theta_H$  increases until 0.67 ML when  $\text{H}_2$  gas is exposed. It can be understood because when the  $\text{H}_2$  gas is adsorbed on the  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$  surface, it will be dissociated into two atoms of H, see Equation (2.1). The H atom coverage will decrease again to zero if the  $\text{H}_2$  gas is switched off.

Figure 10: Coverage of oxygen atom ( $\theta_O$ ) on  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$  surface.

Then, the  $\theta_O$  on the  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$  surface is presented in Figure 10. According to Figure 10, the maximum coverage of the oxygen atom on the  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$  surface is  $1.6 \times 10^{-6}$  ML. The oxygen coverage decreases when the  $\text{H}_2$  gas is exposed. It can be explained by Equation (2.2) and Equation (2.3). When the oxygen gas comes to the  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$  surface, it will be dissociated to be two atoms of oxygen, Equation (2.2). Then each oxygen atom on the  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$  surface will react with two adsorbed atoms of H-producing water molecules on the  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$

surface, which decreases the occupation of the oxygen atom on the  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$  surface. Based on Figure 10, the oxygen coverage is not as much as H coverage (Figure 9). Still, oxygen coverage has more influence on the work function of  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$  because oxygen is a gas that interacts firstly with the surface of  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$ . It means oxygen changes the work function of  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$  at the beginning of the process. Once the oxygen coverage decreases because of the reaction with the incoming H, it causes the work function change of  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$ .

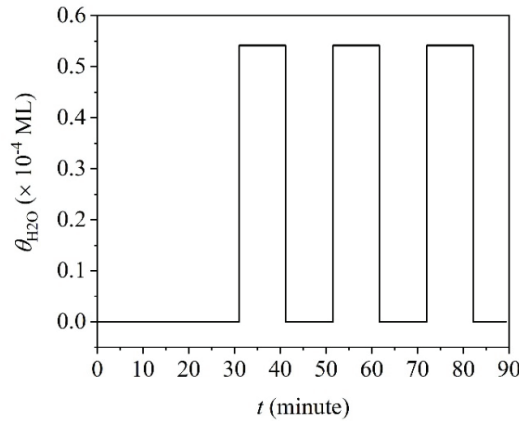


Figure 11: Coverage of water molecule ( $\theta_{\text{H}_2\text{O}}$ ) on  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$  surface.

Finally, this simulation can also calculate the  $\theta_{\text{H}_2\text{O}}$  on the  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$  surface (Figure 11). Based on Figure 11, the water molecule coverage starts with zero. It will not be zero if the adsorption of a water molecule in the air takes place in the calculation. Afterwards, the water molecule coverage increases along with the exposure of  $\text{H}_2$  gas because the adsorbed-oxygen atom and the adsorbed-H molecules react with each other, producing adsorbed-water molecules until  $5.4 \times 10^{-5} \text{ ML}$ .

#### 4. CONCLUSION

This research successfully obtains the unknown values of six parameters of  $\text{H}_2$  gas detection through optimisation and simulation of the detection process by using MATLAB. This simulation can approach the graphic trend of experimental results with a very good approximation. The height of the simulated signal ( $-240 \text{ mV}$ ) is also almost close to the experimental signal ( $-297 \pm 9 \text{ mV}$ ). Other contributions of this study, i.e., it can predict the occupation/coverage of atoms/molecules of gases on the  $\text{Pt}_{80}\text{Au}_{14}\text{Ti}_6$  surface, which another experiment in the laboratory should prove.

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